

The quest to understand and control very short laser light disc – pulses

George Nemeş

- ASTiGMAT, Santa Clara, CA, USA; gnemes@astigmat-us.com
- EE Department, School of Engineering, Santa Clara University, Santa Clara, CA, USA; gnemes98@hotmail.com

OUTLINE

1. INTRODUCTION. BEAMS vs. SHORT LASER DISC – PULSES
2. NEW SPATIAL – TYPE OPTICAL SYSTEMS
3. SPATIAL – TEMPORAL ANALOGY
4. FROM 4x4 SPATIAL MATRICES TO 6x6 or 8x8 SPATIAL – TEMPORAL MATRICES FOR DISC – PULSES
5. PHASE – SPACE SPATIAL – TEMPORAL OPTICS
6. CONCLUSION

1. INTRODUCTION

BEAMS vs. SHORT LASER DISC – PULSES

Goal

- Understanding short laser pulses
- Exploratory approach: Extending concepts from laser beam optics into laser disc – pulses optics

1.1. Regular (stationary) laser beam

1.2. Non – stationary (pulsed) laser beams: beam – pulses

1.3. Extremely short laser pulses: laser disc – pulses

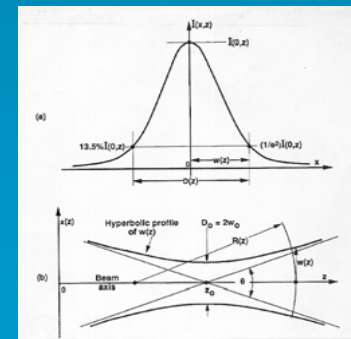
1.1. Regular (stationary) laser beam

Beam concept. Beam = Light distribution that is:

- (Quasi)stationary = time (quasi)invariant = CW or “long” pulse;
 τ – pulse duration; $\tau \rightarrow \infty$ (practically $\tau \geq 1$ ns); **propagation ignored**
- (Quasi)monochromatic: $\Delta\lambda \ll \lambda_0$
- Extends longitudinally on a length L ; $L \in (-l_0, l_0)$, $l_0 \rightarrow \infty$;
 $L = c\tau$; $c = 3 \times 10^8$ m/s;
- Has a waist of diameter D_0 ; $\lambda_0 \ll D_0 \ll L$
- Can be represented as a **paraxial** ($\theta \leq (1/\pi)$ rad) **distribution of rays**

Example: $\lambda_0 = 1064$ nm; $D_0 = 3$ mm; $\tau = (1 - 10)$ ns $\rightarrow L = (300 - 3000)$ mm;

Beams \rightarrow Only **spatial properties** are of interest



1.2. Non – stationary (pulsed) laser beams: beam – pulses

Pulsed – beam (beam - pulse) concept. Beam - pulse = light distribution that is:

- Non-stationary = time dependent = “short” pulse; $\tau = (10 - 1000) \text{ ps}$

Propagation properties – important (**spatial – temporal coupling**)

- Polychromatic: $\Delta\lambda < \lambda_0$

- Longitudinal extent $L \sim (1 - 10)D_0$; $\lambda_0 \ll D_0 \leq L$

- Ray and divergence concepts still apply (with some care)

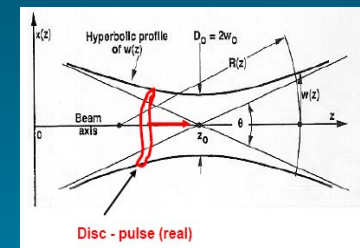
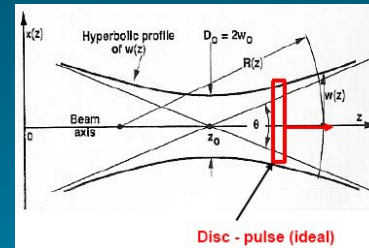
Example: $\lambda_0 = 1064 \text{ nm}$; $D_0 = 3 \text{ mm}$; $\tau = 10 \text{ ps} \rightarrow L = 3 \text{ mm}$;

Beam – pulse \rightarrow **Spatial and temporal properties** are of interest

1.3. Extremely short laser pulses: laser disc – pulses

Laser disc - pulse concept:

- Non-stationary = “extremely short” pulse; $\tau = (0.1 - 10000) \text{ fs}$
- Propagation properties \rightarrow strong spatial – temporal coupling (spatial – temporal astigmatism)
- Extremely polychromatic: $\Delta\lambda \sim \lambda_0$
- Longitudinal extent L ; $\lambda_0 \leq L \ll D_0$



Example: $\lambda_0 = 775 \text{ nm}$; $D_0 = 3 \text{ mm}$; $\tau = 100 \text{ fs} \rightarrow L = 30 \mu\text{m} \rightarrow$ Light disc
Disc – pulse \rightarrow Spatial and temporal properties are of interest

New theory/analysis is necessary

- Ray and divergence concepts \rightarrow need reevaluation. Do they apply?
- Lenses and free-spaces (air) \rightarrow no more close to ideal \rightarrow new analysis
- Spatial – temporal astigmatism can be very strong \rightarrow decoupling

Exploratory approach: Look at existing theory and extend it (if you can!)

Exploratory approach

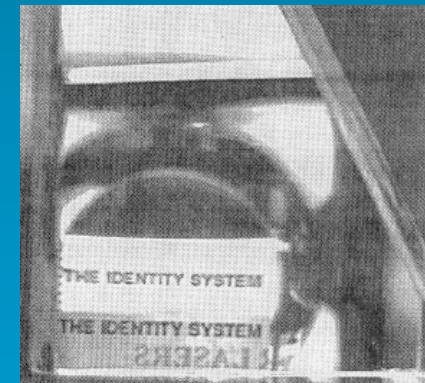
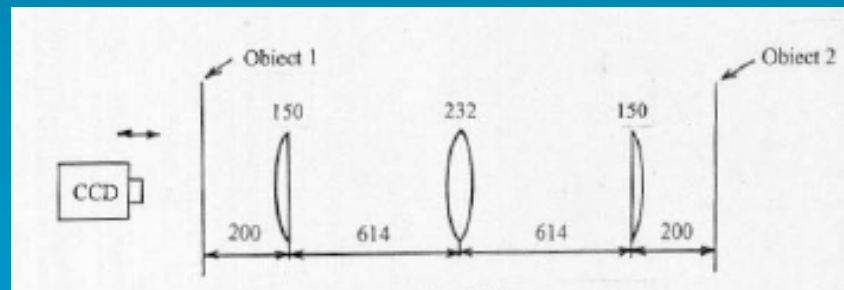
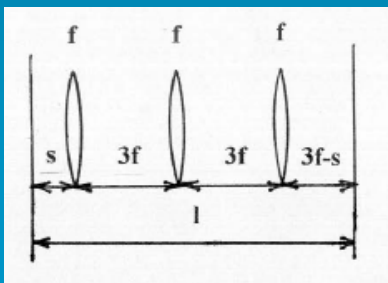
2. NEW SPATIAL – TYPE OPTICAL SYSTEMS

(a) New spatial optical systems with fixed parameters

- Identity $S = I = \{\{1,0\},\{0,1\}\}$
- Pseudo-identity $S = -I = \{\{-1,0\},\{0,-1\}\}$
- Negative space $S = \{\{1,-|d|\},\{0,1\}\}$
- Pseudo-space, pseudo-lens; any physically obtainable ABCD system

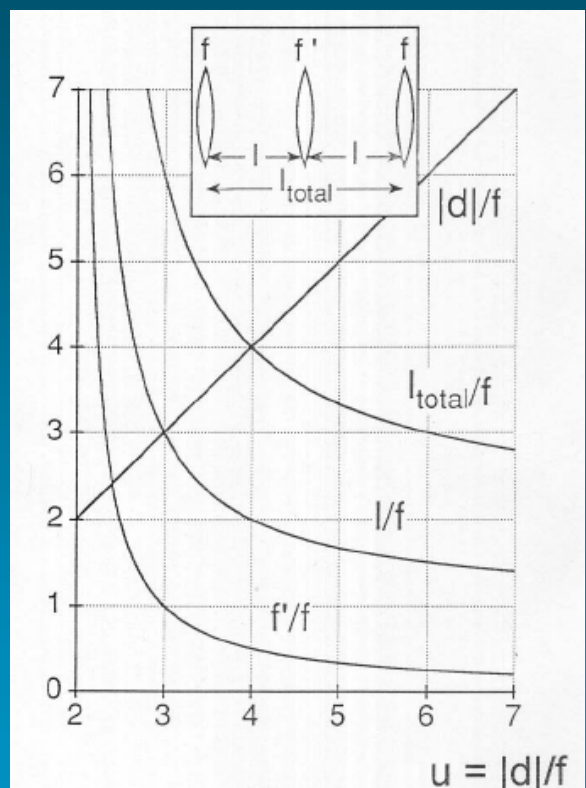
$$S = \{\{A,B\},\{C,D\}\}; AD - BC = 1$$

Examples



Identity

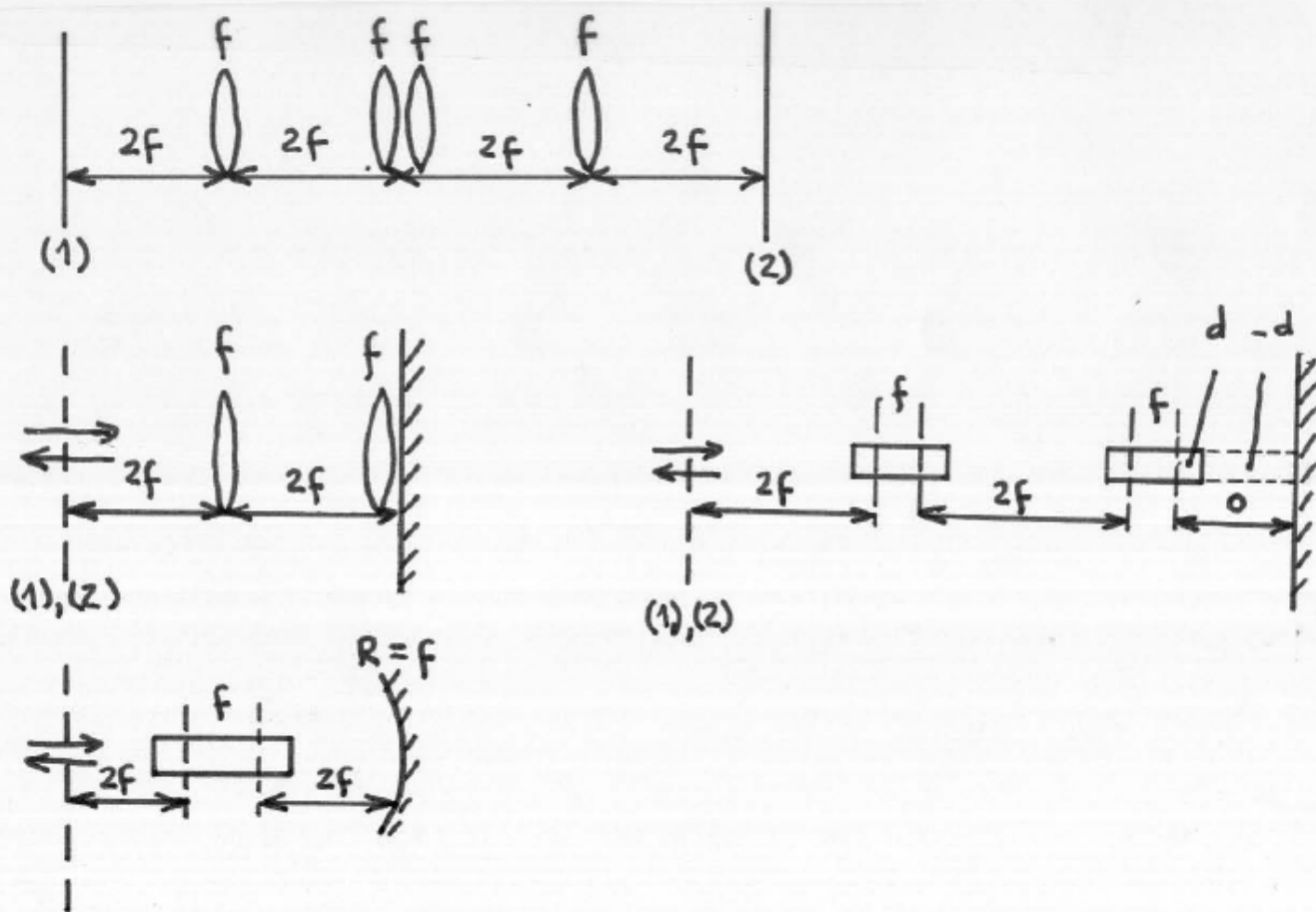
Examples (continued)



Negative space: $|d| = f(2f' + f)/f'$

Suggested application of identity/pseudo-identity

Thermal lens effect compensation in active media



(b) New spatial optical systems with adjustable parameters (zoom)

- **VariSpot[®]** → Round spots, adjustable diameters (20 μm – 30 mm), fixed working distances (25 mm – 5000 mm), $\tau = 150$ fs – CW
- **VariFoc[™]** → Round, square, elongated spots, x,y sizes and working distances independently adjustable
- **VariPol[™]** → Linear polarizer device with adjustable extinction ratio (for VariSpot[®] to get a constant irradiance and variable spot size)
- Other zoom-type configurations: **VariQuad**, **VariSymm**, **VariSpace (1D)**

All are based on **cylindrical optics**

VariSpot[®]

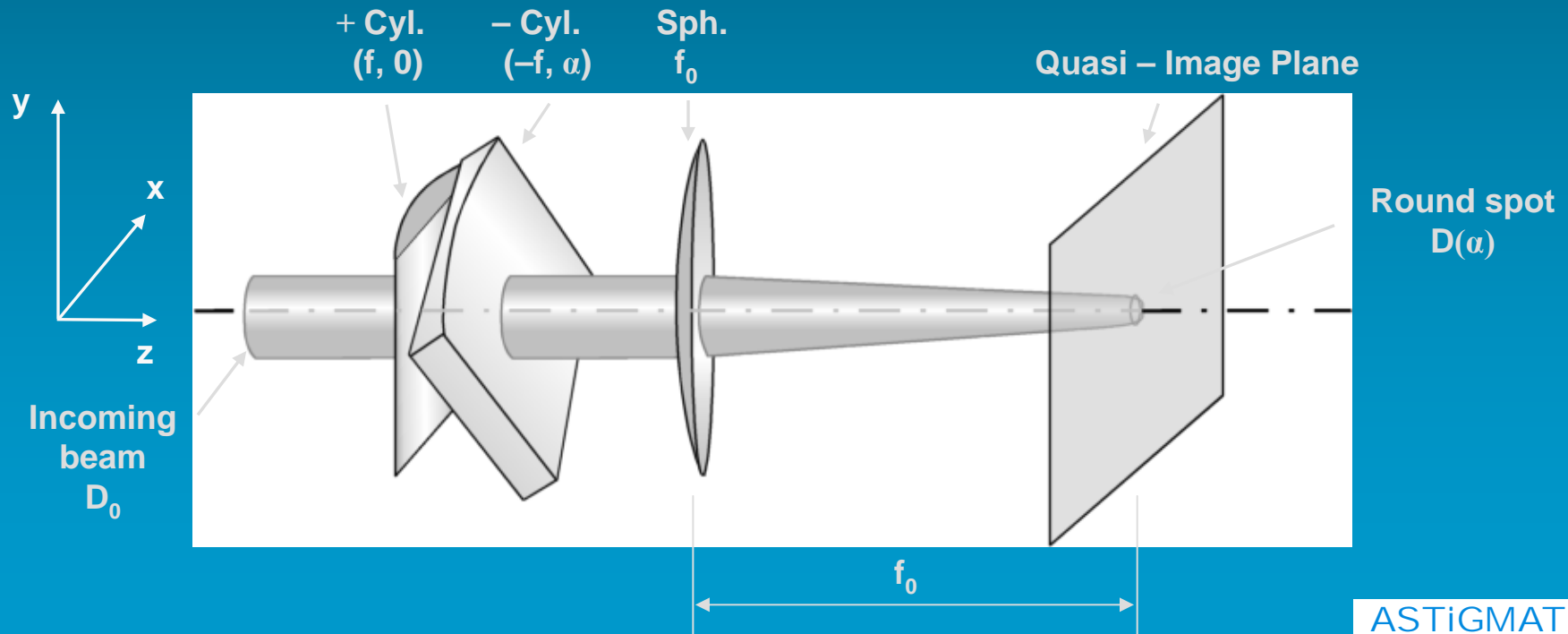
VariSpot[®] - one possible block diagram: short length

3 - lens system:

+ cyl. lens, cyl. axis vertical ($f, 0$)

- cyl. lens, cyl. axis rotatable about z ($-f, \alpha$)

+ sph. lens (f_0) + free-space of length $d = f_0$ (back-focal plane)



VariSpot® - long length version



VariSpot® FL - 140 - VIS

VariSpot® - short length version (industrial)



VariSpot® FS - 400 - 1064

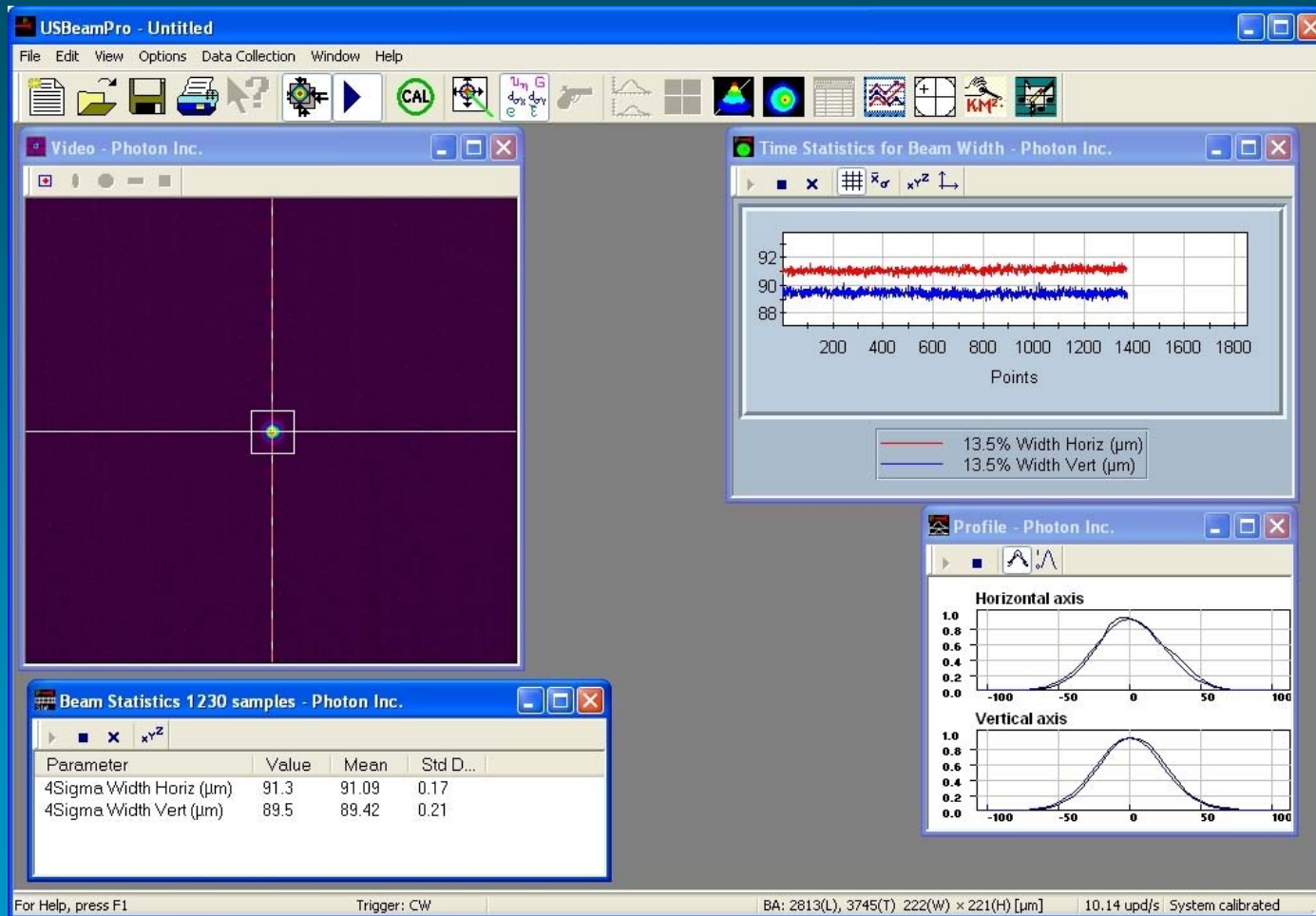
VariSpot® FS-500-1-266



VariSpot® FS-500-1-266 in 266 nm, 30 ps laser beam-pulse

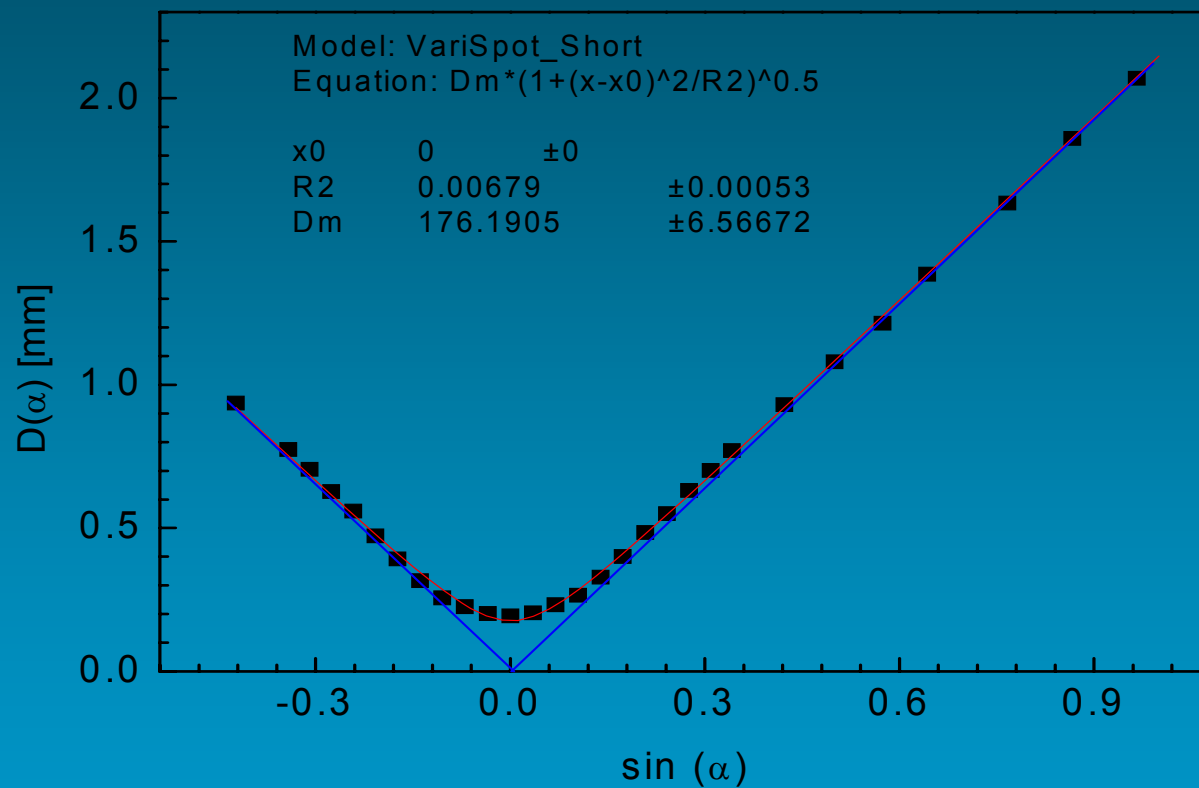


Small spot (0.1 mm) of FS-500-1-266 in He-Ne laser

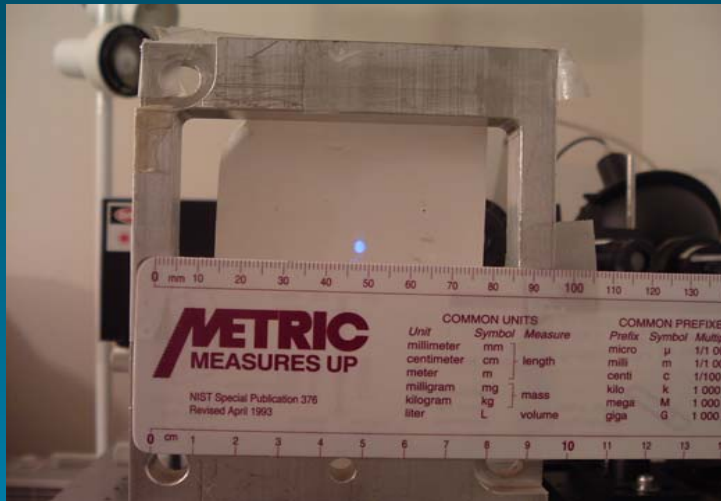


VariSpot® FS 300 -1-UV-NIR in 180 fs laser

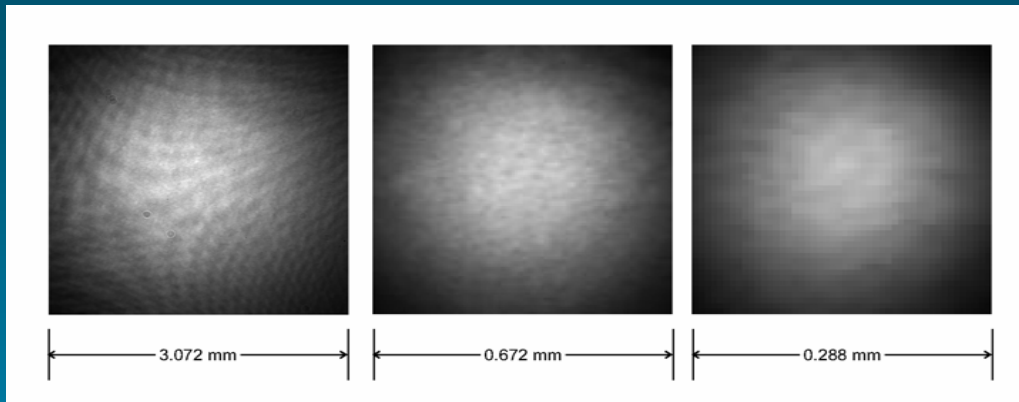
$$D(\alpha) = D_m \left[1 + \frac{(\sin(\alpha) - \sin(\alpha_0))^2}{(f / z_R)^2} \right]^{1/2}$$



VariSpot[®] + N₂ laser (337 nm, UV)



VariSpot[®] image-mode (G. Nemes, J. A. Hoffnagle, "Optical system for variable resizing of round flat-top distributions", Proc. SPIE 6290 (2006))

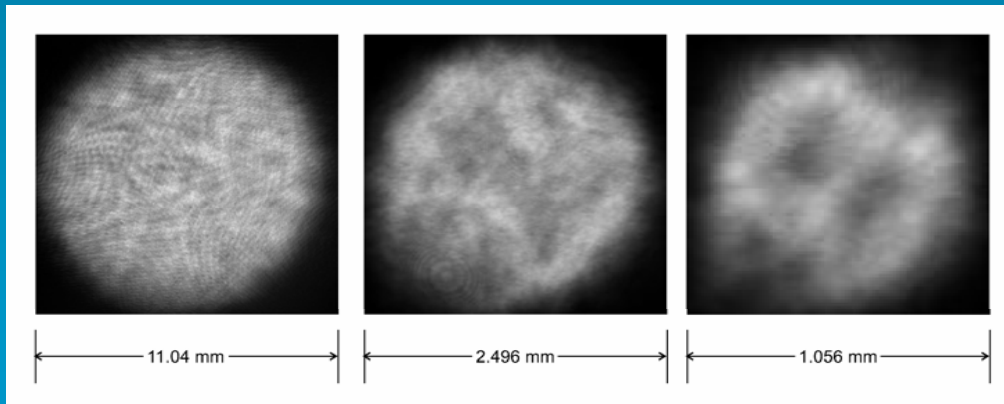
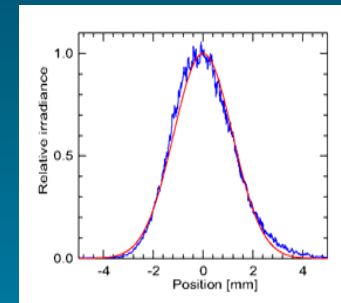


$\alpha = 50^\circ$

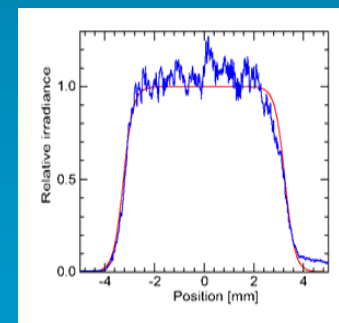
$\alpha = 10^\circ$

$\alpha = 4^\circ$

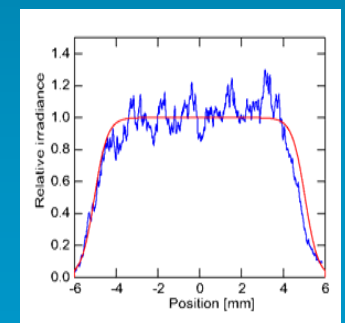
Gaussian beam



Fermi-Dirac (flat-top) beam



Input beam

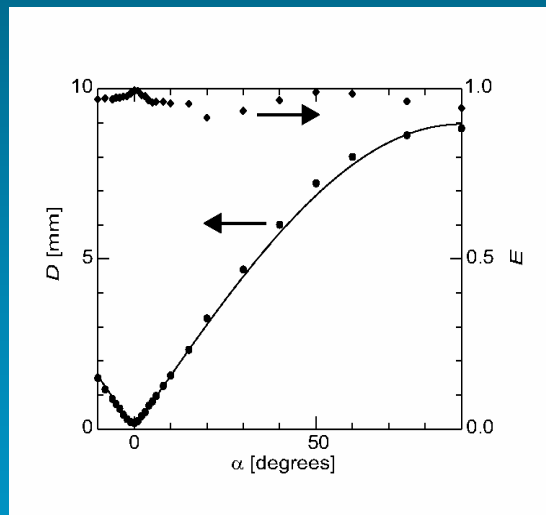


Output beam $\alpha = 50^\circ$

VariSpot[®] - image-mode: Gaussian beam

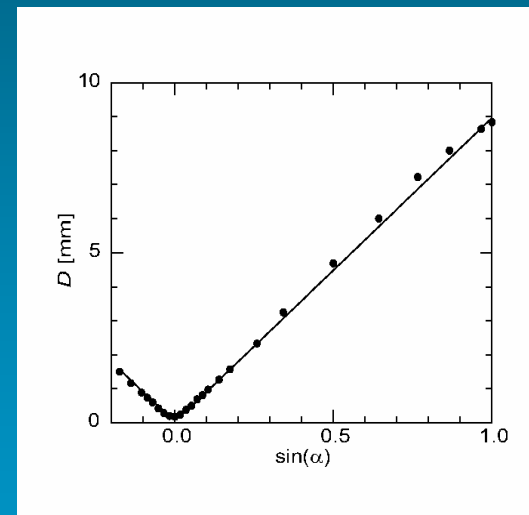
Image-mode $\rightarrow D(\alpha) \approx D_0(f_0/f)\sin(\alpha) = D_M\sin(\alpha)$

Gaussian beam



$D(\alpha)$ vs. α

$E = d_{\min}/d_{\max}$ vs. α

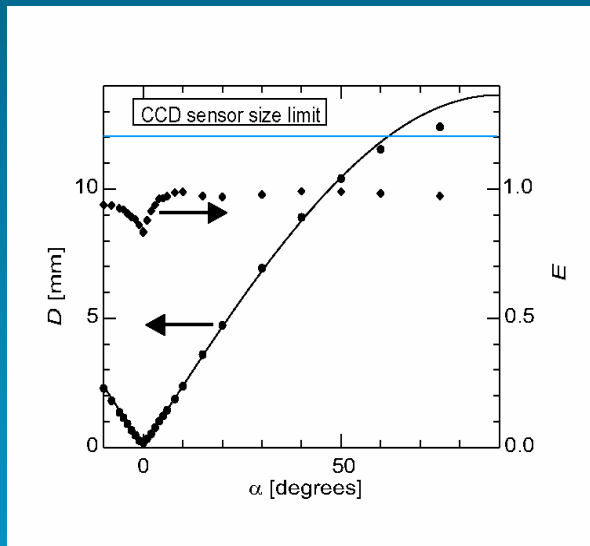


$D(\alpha)$ vs. $\sin(\alpha)$

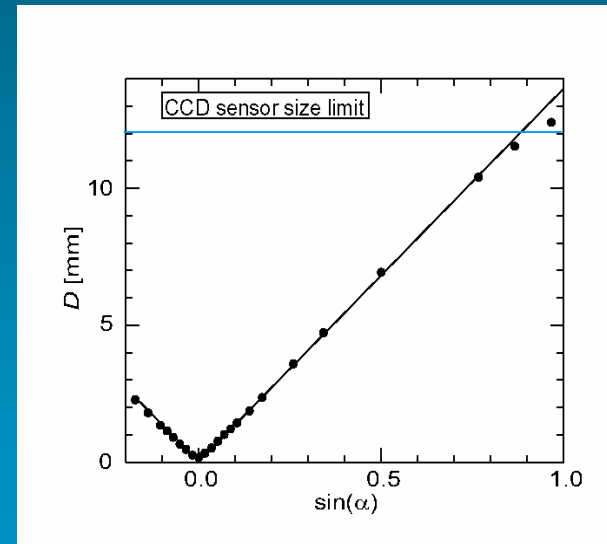
VariSpot[®] - image-mode: Flat-top (Fermi-Dirac) beam

$$\text{Image-mode} \rightarrow D(\alpha) \approx D_0(f_0/f)\sin(\alpha) = D_M\sin(\alpha)$$

Flat-top (Fermi-Dirac) beam



$D(\alpha)$ vs. α



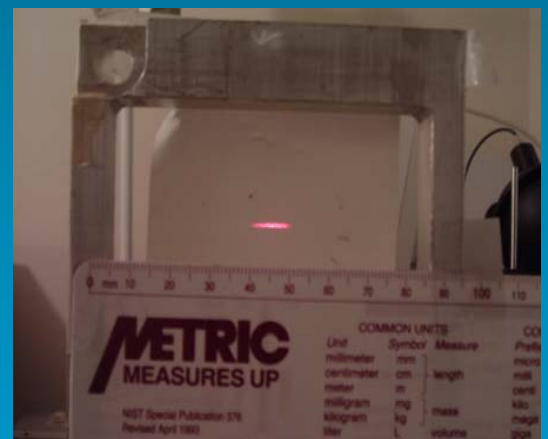
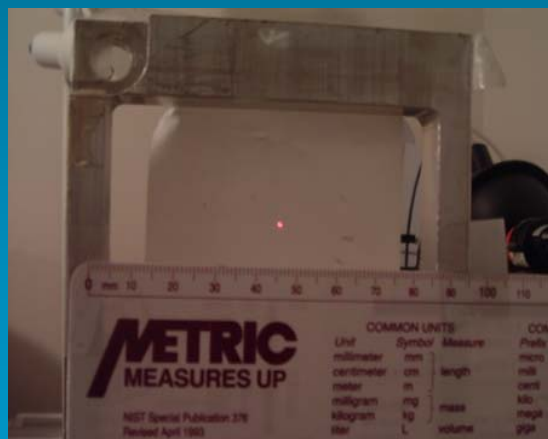
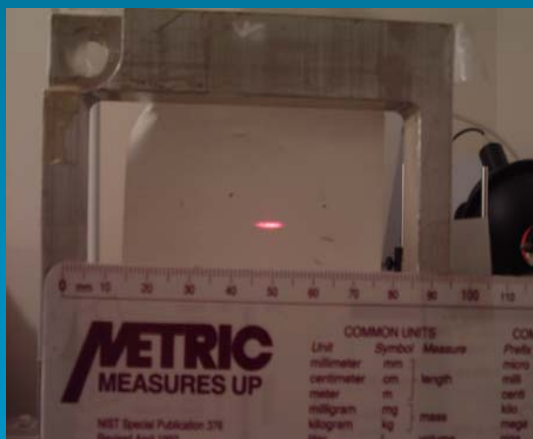
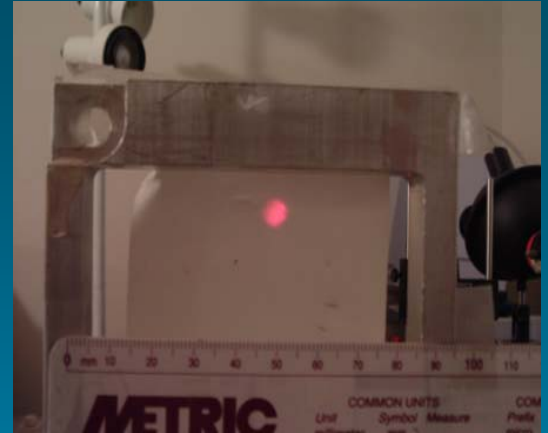
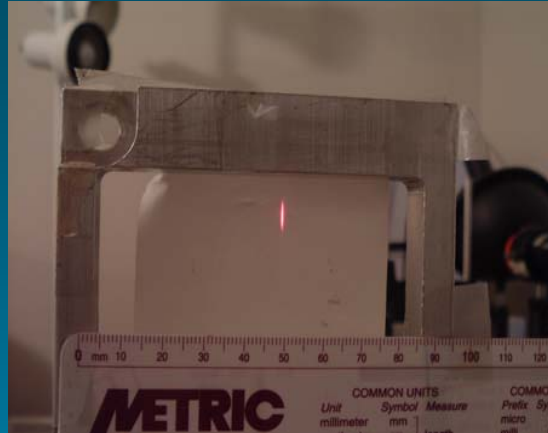
$D(\alpha)$ vs. $\sin(\alpha)$

$$E = d_{\min}/d_{\max} \text{ vs. } \alpha$$

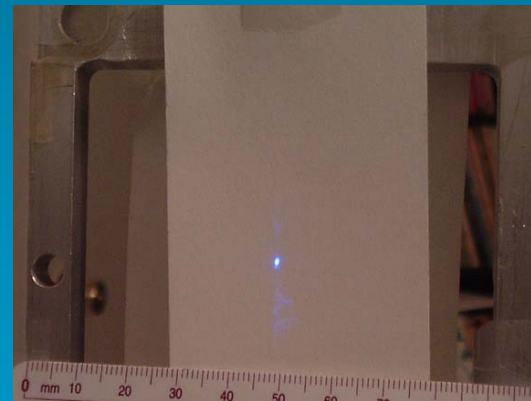
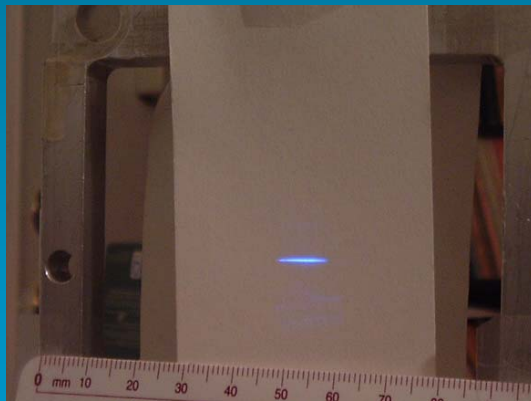
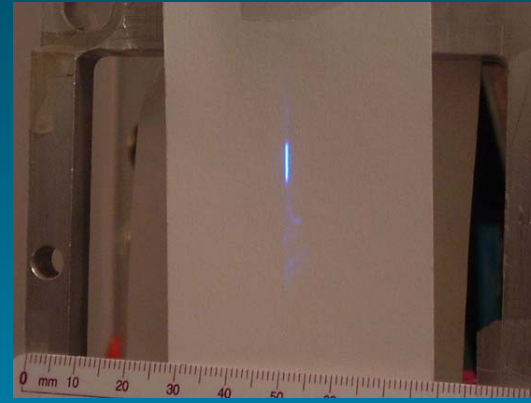
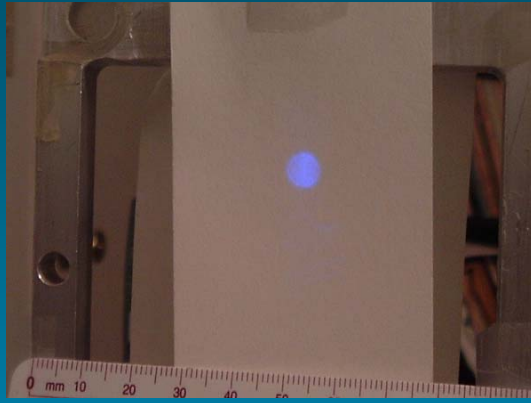
VariFoc™ – demo unit



VariFoc™ + collimated diode laser (670 nm)



VariFoc™ + N₂ laser



3. SPATIAL – TEMPORAL ANALOGY

Known spatial – temporal analogy (Akhmanov; Froehly, Martinez; Dijaili; Kostenbauder; Kolner; Nazarathy; Yariv; Godil; Trebino; and others)

Spatial lens \rightarrow temporal lens (quadratic temporal phase modulator)

Spatial free-space (spatial diffraction) \rightarrow temporal dispersion (in fibers)

k_x (spatial frequency) \rightarrow ω (temporal frequency)

x (transverse coordinate) \rightarrow $t - z/v_g$ (time, moving reference frame)

$1/k$ (wave vector reciprocal) \rightarrow $-\beta''$ (GVD coefficient)

2x2 spatial matrix optics \rightarrow 2x2 temporal matrix optics

4x4 (2 spatial + 2 temporal) matrix optics

6x6 (4 spatial + 2 temporal, decoupled from spatial) matrix optics

Suggestion: Finding the temporal matrices analog to the new spatial 2x2 matrices

4. FROM 4x4 SPATIAL MATRICES TO 6x6 or 8x8 SPATIAL – TEMPORAL MATRICES FOR DISC – PULSES

Existing results in **4x4 spatial matrix optics** (Nemes, Siegman, Serna)

- Classification and identification of any ABCD matrix representing an optical system (stigmatic - ST; aligned simple astigmatic - ASA; rotated simple astigmatic - RSA; general astigmatic - GA)
- General and constructive synthesis procedure for any 4x4 ABCD-type spatial optical system physically obtainable
- Geometrical classification and identification of any 4x4 **P** matrix representing a physical beam (ST; ASA; RSA; GA, including degeneracies)
- Obtaining the general beam invariants at transformation through spatial optical systems in 4x4 matrix treatment: **intrinsic astigmatism, a** ;
maximum intrinsic astigmatism, a_M ; $0 \leq a \leq a_M$
- General, constructive procedure to decouple any beam (GA \rightarrow ASA or ST)

Suggestion:

- Existing (complete) 4x4 matrix theory for spatial optical systems and beams → 6x6 (?) or 8x8 (perhaps) matrix theory for spatial – temporal optical systems and disc – pulses (including spatial – temporal invariants, general astigmatism and decoupling)
- Looks appealing but not easy!

5. PHASE – SPACE SPATIAL – TEMPORAL OPTICS

Existing results (Liouville; Boltzmann; Hamilton; Wigner; Ville; Lapostolle; Lawson; E. Wolf; Bastiaans; Lohmann; Brenner; K.B. Wolf; G. & M. Nemes; Ozaktas; Dragoman; and others)

Types of phase-spaces (PS) used in optics and signal theory:

2-D, spatial-type $\rightarrow (x, \theta); (x, k_x)$

2-D, temporal type $\rightarrow (t, \omega)$

4-D, spatial-type $\rightarrow (x, y, \theta_x, \theta_y); (x, y, k_x, k_y)$

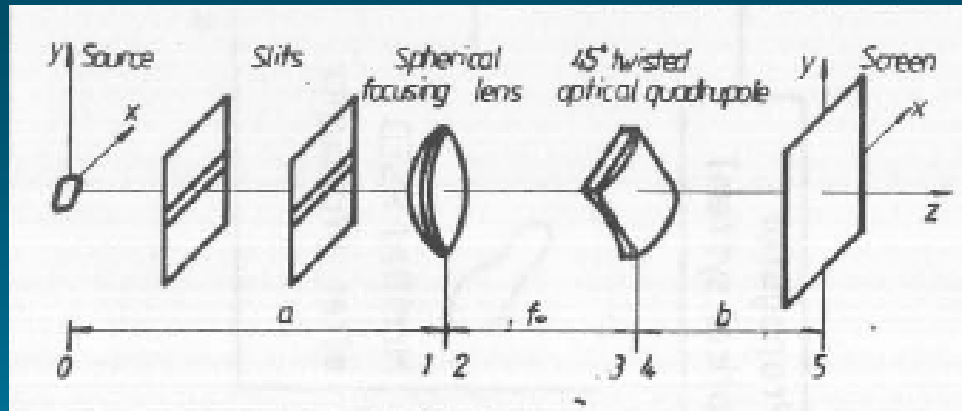
4-D, spatial 2-D + temporal 2-D $\rightarrow (x, t, \theta, \omega)$

6-D, spatial 4-D + temporal 2-D $\rightarrow (x, y, t, \theta_x, \theta_y, \omega)$

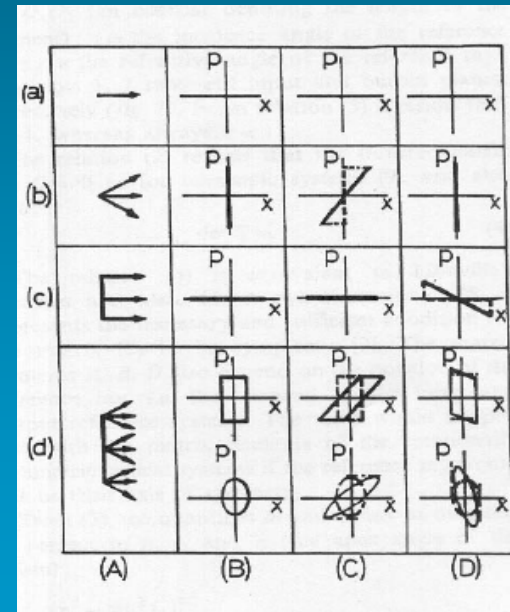
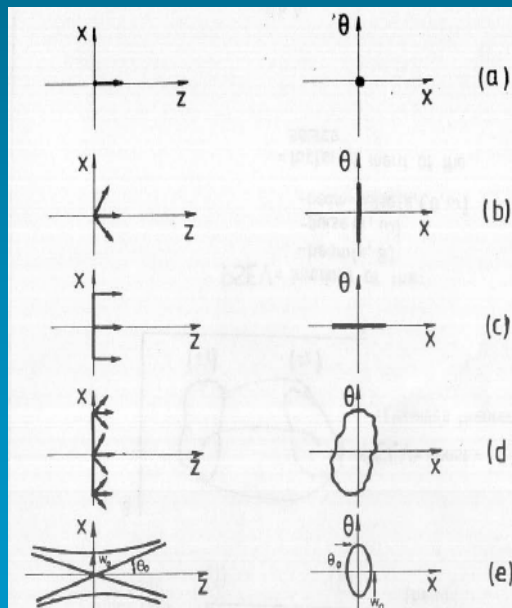
Note: The optical systems act as phase-space transformers on appropriate rays or ray-pulses (corresponding to the PS dimension)

Liouville – Boltzmann theorem: lossless and gainless systems preserve the PS measure (“volume”)

Original experiments in Spatial 2-D Phase-Space (PS)

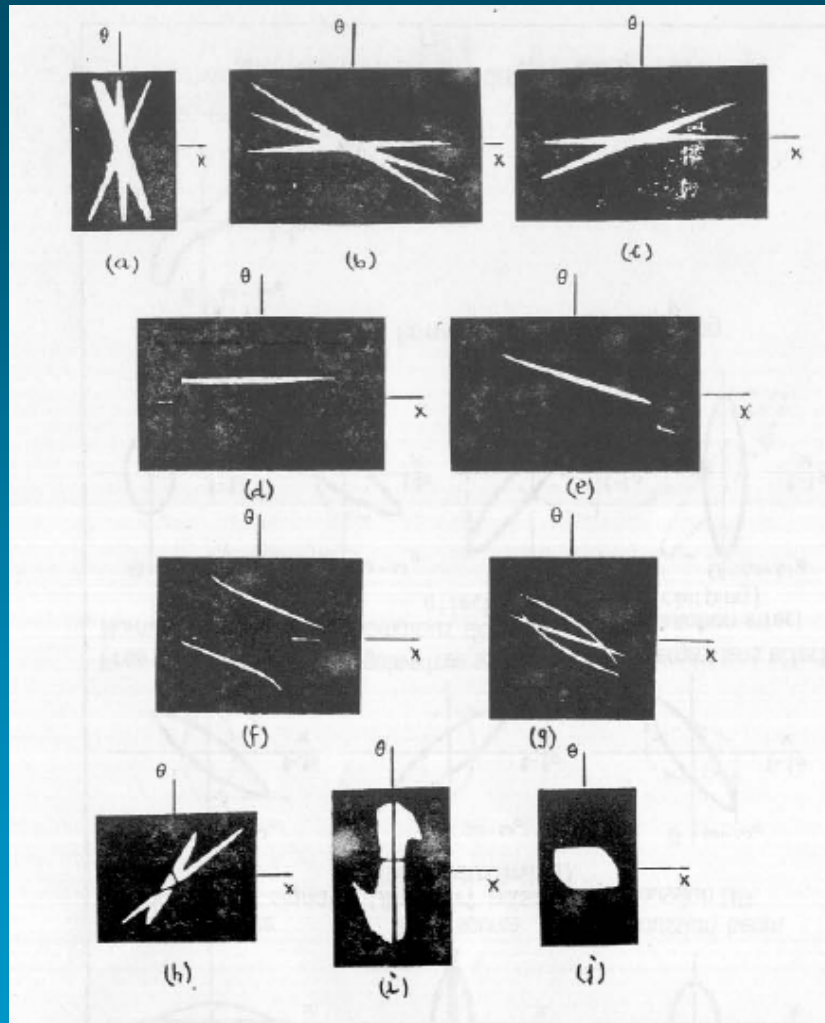


Experimental set-up



Ideal and real light sources and their transformation through free-space and lens, in PS

Original experiments in Spatial 2-D Phase-Space



- (a) Point source, free-space
- (b) Plane wave, convergent lens
- (c) Plane wave, divergent lens
- (d) Prism effect on plane wave
- (e) Prism effect on convergent beam
- (f) Spherical aberrations, (+) lens
- (g) Comma-type aberrations, (+) lens
- (h) Liouville-Boltzmann theorem, free-space and large "PS volume" source
- (i) Spherical aberrations of (+) lens, large "PS volume" source
- (j) PS filtering: PS device acceptance boundary (in very large "PS volume" source)

- Suggestions:

Extending the phase-space approach to treat laser disc – pulses,
by using spatial – temporal analogy

- Needs:

New theory

New experiments

6. CONCLUSION

- Short laser pulses need a reconsideration of classical geometrical and physical optics concepts: ray, optical system, beam → disc – pulse concept
- The new, original results of treating spatial optical systems and laser beams using 2×2 and 4×4 spatial matrices might be extended to treat laser disc – pulses using 8×8 matrices
- Simple concepts and experiments in 2-D spatial phase-space might be extended in higher – dimensional phase-spaces associated to disc – pulses
- The expected results might justify the theoretical and experimental efforts
 - Newcomers in the field are welcome!